

Abell 43: Longest Period Planetary Nebula Nucleus Variable[★]

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ABSTRACT

Context. Most PG 1159 stars are hydrogen deficient post-AGB stars on their way to the white dwarf cooling sequence. However, a fraction of them show small amounts of atmospheric hydrogen and are known as the hybrid PG 1159 stars. Both the normal and hybrid PG 1159 stars may reside at the centre of a Planetary Nebula. Some PG 1159 stars exhibit non-radial g -mode pulsations, providing us with a means to constrain their fundamental physical parameters, internal structure, and evolutionary status; asteroseismology is the technique of using global stellar pulsations to probe the star's interior.

Aims. Model calculations demonstrate that the PG 1159 instability strip is driven by the partial ionization of carbon and oxygen through the κ -mechanism. The range of excited frequencies in models is sensitive to the details of the chemical composition in the driving zone. Hydrogen content plays a crucial role in deciding the range of excited frequencies for models of hybrid PG 1159 pulsators. The range of periods observed in all PG 1159 pulsators can then be compared against the range predicted by theoretical models, which are based on observations of their chemical composition and evolutionary status. Our aim is to test the validity of the predicted range of pulsation periods for the hybrid PG 1159 variables, Abell 43 and NGC 7094.

Methods. To achieve this goal, we acquired continuous high speed CCD photometry of the hybrid PG 1159 star Abell 43 using the 2.6 m Nordic Optical Telescope and the 3.5 m telescope at Apache Point Observatory. We also observed NGC 7094, a hybrid PG 1159 star with atmospheric parameters similar to Abell 43. We analyzed our data to obtain the pulsation spectra of the two stars.

Results. We detected six significant pulsations in the light curves of Abell 43 with periods between 2380 s and 6075 s. We were also fortunate to detect low amplitude pulsations in our NGC 7094 data with periods between 2000 s and 5000 s. The observed range of periods for both stars is consistent with the theoretical predictions.

Conclusions. The range of periods observed in both hybrid PG 1159 stars, Abell 43 and NGC 7094, agree with the theoretical model that the pulsations are driven by the κ -mechanism induced by the partial ionization of carbon and oxygen.

Key words. stars: planetary system - stars: oscillations - stars: individual: Abell 43, NGC 7094 central star.

1. Introduction

Hydrogen deficient hot white dwarf stars constitute the PG 1159 class, and are often found at the centre of planetary nebulae. Abell 43 (= WD 1751+10) is one of the four known hybrid PG 1159 stars, which show evidence of a non-negligible hydrogen abundance in their atmospheres (Napiwotzki & Schönberner 1991). Miksa et al. (2002) recently published the following atmospheric parameters for Abell 43: $T_{\text{eff}} = 110 \text{ kK}$, $\log g = 5.7$, $X(\text{H}) = 0.35$, $X(\text{He}) = 0.42$, and $X(\text{C}) = 0.23$ in mass fractions. Werner & Herwig (2006) found an even higher carbon abundance from HST ultra-violet observations of Abell 43.

Low carbon abundance determinations by Dreizler et al. (1995) had initially led Quirion et al. (2004) to rule out pulsations in Abell 43 based on their model calculations. But the recent high carbon abundance measurements led Quirion et al. (2005) to re-evaluate their previous conclusions about Abell 43. They found that the revised models suggested that Abell 43 should exhibit $\ell = 1$ g -mode pulsations, driven by the classical κ -mechanism due to the ionization of carbon K-shell electrons, in the range of ~ 2604 – 5529 s. Córscico et al. (2006) carried out nonadiabatic pulsation calculations for a grid of evolutionary PG 1159 models. They predicted that Abell 43 should exhibit periods in the range of ~ 2600 – 7000 s adopting a $0.530 M_{\odot}$ stellar mass evolutionary track.

Ciardullo & Bond (1996) were the first to report possible variations in the light curve of Abell 43 with a period of about 2473 s. Schuh et al. (2000) detected a longer period of 5500 s. They also suggested that the ~ 2500 s period reported by Ciardullo & Bond (1996) could simply be an artifact of the 5500 s period caused by the short duration of the observations.

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[★] Based on observations made with the Nordic Optical Telescope, operated on the island of La Palma jointly by Denmark, Finland, Iceland, Norway, and Sweden, in the Spanish Observatorio del Roque de los Muchachos of the Instituto de Astrofísica de Canarias.

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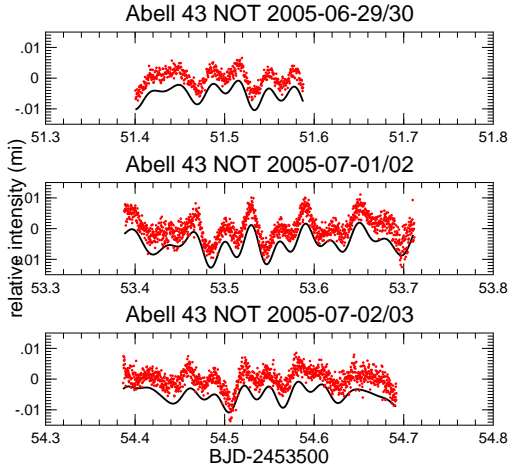


Fig. 1. Light curves of Abell 43 shown for the three long NOT runs. The solid lines are synthetic light curves constructed from the parameters listed in Table 2, and shifted downward by 0.005 units for clarity.

Table 1. Log of observations of Abell 43

Date	Start (UT)	Length (hrs)	Cycle time(s)	Data points	Observer
2005-06-29	21:28	4.40	30	541	JES ^a
2005-07-01	03:43	1.56	20	283	JES
2005-07-01	09:14	1.54	37	51	ASM ^b
2005-07-01	21:08	7.71	20	1399	JES
2005-07-02	21:07	7.32	20	1319	JES
2005-07-10	07:24	1.71	41	110	ASM

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Vauclair et al. (2005) discovered multiple modes in the pulsation spectrum of Abell 43, and reported periods at 2600 s and 3035 s. Their observations were based on three individual runs, amounting to a net observation time of 7.5 hr at the 2.6 m Nordic Optical Telescope (NOT).

In this paper, we report the results from 24 hours of time-series photometry acquired on Abell 43 in 2005 with the 2.6 m NOT and the 3.5 m telescope at Apache Point Observatory (APO). We also report pulsation periods detected in the hybrid PG 1159 star NGC 7094 (= WD 2134+125), which is almost like a spectroscopic twin of Abell 43.

2. Observations

We observed Abell 43 for four nights, from the 29th of June to the 2nd of July, 2005 using the 2.6 m NOT in addition to two short runs with the 3.5 m telescope at APO on the 1st and 10th of July, 2005. The log of observations is given in Table 1.

We conducted observations at the NOT using the Andalucia Faint Object Spectrograph and Camera (ALFOSC), which is equipped with a thinned 2048 × 2048 E2V CCD 42-40 chip. We observed with the broadband blue W92 filter, which has a FWHM of 275 nm centered at 550 nm; this enables us to gather a fair amount of flux from the target and minimize the sky contribution at the same time. We acquired suitable flat fields each night just after sunset and determined the dark current for each individual image using the overscan region. We controlled the ALFOSC data acquisition using the software interface *tcpcom*,

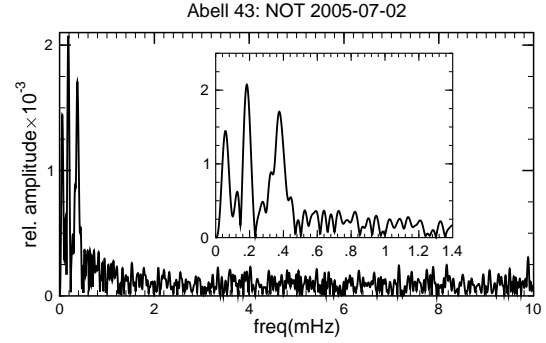


Fig. 2. Pulsation spectrum of the light curve of the NOT run from the 2nd of July, 2005. The insert is a blow up of the low frequency region, that shows the evident lack of excited frequencies above 0.5 mHz.

defining multiple windows to achieve fast readouts (Østensen 2000). We achieved a net readout time of 4.8 to 5.8 s for the six separate windows around the target star, three comparison stars, and two blank fields for determining the simultaneous sky brightness. We chose a time resolution of 30 s during our first night at the NOT telescope, and our exposure time became 23.9 s. We reduced the cycle time to 20 s on subsequent nights, and achieved exposure times of about 14.1, 14.8, and 14.9 s for slightly different windowing patterns. With real time processing, we were able to display light curves of the raw and sky-subtracted data during acquisition.

We followed the standard basic reduction procedure, subtracting a dark frame from each image and then flat-fielding it. After these preliminary steps, we computed light curves using aperture photometry for several aperture sizes. We selected the best light curve based on the highest S/N ratio. For the observations outlined above, we obtained the best result for an aperture diameter of 24 pixels corresponding to 4.6 arcseconds on the sky. We corrected for transparency variations and differential extinction by dividing the target star light curve with the average light curve of the comparison stars. In Fig. 1 we show the light curves from the three longest NOT runs.

The APO observations were acquired with the Seaver Prototype Imaging camera (SPICam) and a Johnson B filter. We used 3 × 3 binning and windowing in order to reduce the read out time to about 25–35 s. The instrument has a read noise of 5 electrons RMS, a gain of 1 e/ADU, and a plate scale of 0.42 arcsec/pixel with 3 × 3 binning. We used a standard IRAF reduction to extract sky-subtracted light curves from the CCD frames using weighted circular aperture photometry (O’Donoghue et al. 2000).

3. Hybrid PG 1159 star Abell 43.

3.1. Single night observations

We initially computed Discrete Fourier Transforms (DFTs) of the three long light curves acquired using the NOT. We show only the DFT from one of the longest runs in Fig. 2, as the other DFTs look similar. We list the following observed features evident from the DFTs of our NOT data:

- Each pulsation spectrum shows three dominant components, which are relatively stable in frequency, but exhibit variable amplitudes.

Table 2. Identified periodic signals in Abell 43 in the three long NOT runs

Date	Res.	F1	P1	A1	F2	P2	A2	F3	P3	A3	F4	P4	A4	F3/F1
2005	(μ Hz)	(μ Hz)	(s)	(mma ^a)	(μ Hz)	(s)	(mma)	(μ Hz)	(s)	(mma)	(μ Hz)	(s)	(mma)	
06-29	63	183.3	5456	2.0				363.9	2748	2.3	416.3	2402	0.8	1.98
σ		1.4	41	0.1				1.2	10	0.1	3.6	21	0.1	
07-01	36	175.5	5698	3.1	321	3118	1.0	366.4	2729	2.7	408.3	2449	1.4	2.08
σ		1.2	38	0.1	3.4	34	0.1	0.9	10	0.1	3.4	15	0.1	
07-02	38	185.2	5399	2.1	325	3075	0.8	368.8	2711	1.9	418.9	2387	2.0	1.99
σ		1.6	47	0.1	4.4	41	0.1	1.8	1.4	0.1	3.3	19	0.1	

^a relative amplitude $\times 10^{-3}$

- All pulsation spectra have a strong high frequency cut-off above 0.5 mHz, beyond which we do not detect any signals.
- The light curves are non-stationary¹ and we have to be cautious in drawing conclusions using standard tools for spectral analysis.

The dramatic cut off implies that we only find pulsations with periods longer than ~ 2000 s, as predicted both by Quirion et al. (2005) and Córscico et al. (2006). We determined the frequencies, amplitudes, and phases of the significant peaks in the pulsation spectra using a simultaneous non-linear least squares fit (*Period04*; Lenz & Breger 2005). To determine which peaks in the DFT constituted real power, we used the method of prewhitening in conjunction with the non-linear least squares analysis. This involves fitting the dominant component and subtracting it from the light curve. If we now compute a DFT of this resultant light curve, the peak corresponding to the dominant mode will be absent. We repeat the procedure for the next highest peak in the pre-whitened DFT, fitting both high-amplitude components simultaneously and then subtracting them from the light curve. The resultant DFT will not show power due to both the highest and second-highest peaks. We continue this process as long as there are well-resolved peaks in the DFT. When the prewhitened DFT does not show any significant power, then we can be sure that we have determined the entire pulsation spectrum using the simultaneous non-linear least squares fit. Fig. 3 serves as a demonstration of the prewhitening method.

We show the results of our analysis for the three longest NOT runs in Table 2, that list the significant periods detected with a False Alarm Probability better than 1/100 (Scargle1982). The uncertainties listed in the table are 1σ errors from the non-linear least squares fit. Fig. 1 also includes the synthetic light curves constructed from the frequencies, amplitudes and phases determined as above.

It is evident from Table 2 that F1 varies most in frequency and amplitude from night to night. These variations may be caused by unresolved power. We also notice that the ratio of the frequencies F3:F1 is very close to two on the first and third nights, insinuating a harmonic ratio. The ratio is close to 2.08 on the second night and may perhaps be due to F1 being an unresolved multiplet.

If we compare the periods we detect to those observed earlier, we find that the period 2473 s discovered by Ciardullo & Bond(1996) is close to P4, while the period of 5500 s found by Schuh et al. (2000) is close to P1. The two periods 2600 and 3035 s, discovered by Vauclair et al. (2005) are not too far from P3 and P2. The discrepancies may either be due to insufficient

¹ When signals detected in a light curve are not present for its entire duration, it is said to be non-stationary in nature.

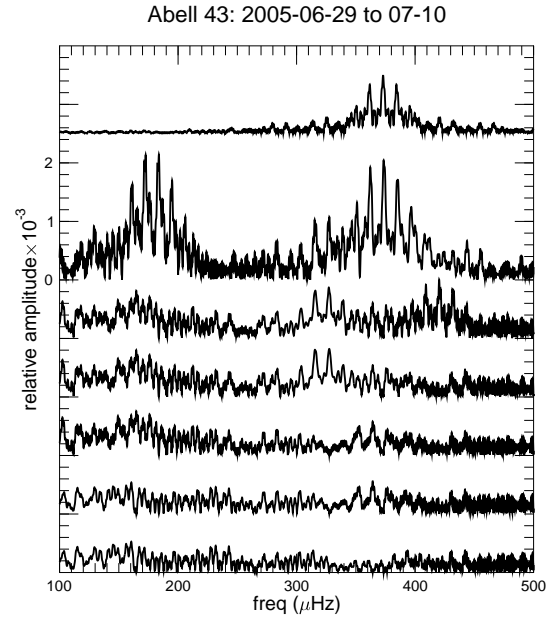


Fig. 3. We show the DFT computed from the combined light curve of five runs used in the analysis. The top curve shows the window function. The second curve shows the DFT of the light curve. The third curve shows the DFT after subtracting out the two highest amplitude peaks. The lower four curves show the DFT after subtracting three, four, five, and six frequencies respectively.

resolution or may perhaps indicate real period changes between the different pulsation modes.

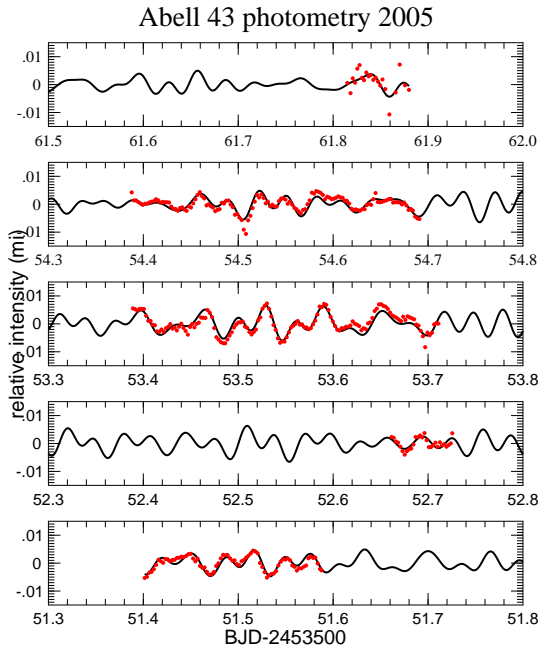
3.2. Combining all useful observations

To investigate whether the nightly variations in frequencies and amplitudes were due to unresolved peaks, we re-analyzed the combined light curves with the addition of the APO observations from the 10th of July, 2005. Note that we could not utilize the APO observations from the 1st of July as bad weather rendered them far too noisy for inclusion in our analysis.

We computed a combined DFT again, and used the prewhitening technique in conjunction with the non-linear least squares analysis to arrive at the values listed in Table 3. We show our final DFT in Fig. 3, along with the different stages

Table 3. Identified periodic signals in Abell 43 from the combined data set

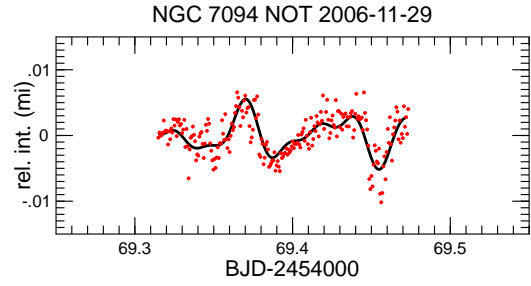
Name	Freq (μHz)	Period (s)	Amplitude (mma ^a)	Noise (mma)
f1	164.62	6075	0.8	0.15
σ	0.08	3	0.1	
f2	183.76	5442	1.9	0.15
σ	0.03	1.0	0.1	
f3	327.70	3051.6	0.9	0.20
σ	0.07	0.7	0.1	
f4	363.79	2748.8	0.9	0.20
σ	0.08	0.6	0.1	
f5	373.12	2680.1	2.0	0.20
σ	0.03	0.2	0.1	
f6	420.23	2379.7	1.0	0.20
σ	0.06	0.4	0.1	

^a relative amplitude $\times 10^{-3}$ **Fig. 4.** We show observed light curves, averaged over a sampling time of 200 s, compared with synthetic curves constructed from parameters in Table 3.

of prewhitening. We find that the power seen earlier as F1 split into two individual frequencies f1 and f2, while the power at F3 split into f4 and f5. Using the new frequency components, we find that $f3/f1 = 1.991$ and $(f4 + f5)/2f2 = 2.005$, giving us two ratios of frequencies close to 2.

Averaging the observations to a sampling time of 200 s, we show the observed light curves along with the synthetic light curves constructed from our fit in Fig. 4; an inspection of this figure reveals that the fit is quite good. This tells us that Abell 43 is more stable than the pulsating PNNi with shorter periods, investigated by González Pérez et al. (2006). We also notice how the light curve can change dramatically on short time scales due to beating of the closely spaced modes; this suggests observations over a shorter time span compared to the beat cycle may give wrong results or show no pulsations at all.

The shortest period we detect in our data is 2380 s, which is quite close to the predicted lower limit of 2600 s for $\ell = 1$

**Fig. 5.** We show the observed light curve of NGC 7094 with a simulated light curve based on the periods 34, 50, and 83 min.

g -mode pulsations induced by the κ -mechanism (Quirion et al. 2005 and Córscico et al. 2006). The longest period of 6075 s is slightly longer than predicted by Quirion et al. (2005) but within the range predicted by Córscico et al. (2006). The non stationary nature of the light curves makes it difficult to draw certain conclusions about the frequency ratios close to 2.00. They may indicate simple harmonics or non linear resonances as proposed by Buchler et al. (1997).

4. Hybrid PG 1159 star NGC 7094: Almost a spectroscopic twin of Abell 43

The hybrid PG 1159 star NGC 7094 shows almost the same spectroscopic parameters as Abell 43, except that 1% He in Abell 43 has to be replaced by 1% O (Miksa et al. 2002). Quirion et al. (2005) propounded that NGC 7094 should pulsate with periods in the range of 2550 - 5413 s. Previous searches by Ciardullo et al. (1996) and González Pérez et al. (2006) did not reveal any pulsations in the star. The latter observation lasted only 5220 s and was probably too short to detect pulsations in the predicted range.

In order to scrutinize the variability of NGC 7094, we asked for a service run on the NOT, which can be a maximum of 4 hr long. We obtained a light curve of length 13692 s with ALFOSC on the 29th of November, 2006. We used the B filter and a window of size $1\text{k} \times 1\text{k}$ pixels. We chose an exposure time of 30 s and the readout time was about the same, giving us a time resolution of 60 s. Fig. 5 shows the light curve we obtained from our observations. With the false alarm probability criterion of 1/100 or better, we identified three peaks with periods between 2000 s and 5000 s. A synthetic light curve constructed from these peaks is also shown in Fig. 5. Longer observing runs are needed to characterize the pulsations better, but this paper serves to establish NGC 7094 as a low-amplitude pulsator.

The range of pulsation periods is shifted toward shorter periods relative to Abell 43. This is predicted by Quirion et al. (2005) and is a consequence of adding a trace of oxygen in their models. The observed lower period limit of 2000 s is shorter than the theoretical limit of 2550 s predicted by the same authors.

5. Conclusions

For the hybrid PG 1159 star Abell 43, we find six pulsation periods with a range close to that predicted for $\ell = 1$ g -mode pulsations driven by the κ -mechanism due to partially ionized carbon (Quirion et al. 2005; Córscico et al. 2006). The light curves are non stationary, but the pulsation frequencies and amplitudes are relatively stable during the 11 day span of the observations.

This is different from pulsating PNNi, which showed changes in amplitudes from night to night, and also during the same night (González Pérez et al. 2006).

We have also detected pulsations in the hybrid PG 1159 star NGC 7094 which is an approximate spectroscopic twin of Abell 43. The observed pulsations lie in the range of 2000–5000 s, in a band of periods shifted to shorter values than for Abell 43. This agrees with theory and occurs when a small amount of oxygen is added to the model pulsator (Quirion et al. 2005), although the lowest period observed is somewhat shorter than predicted for NGC 7094.

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